|                | Question for Mathematics Programme students: Full Marks = 10<br>G - CC - T - 04  | 10           |
|----------------|--|--------------|
|                | Answer any 2 (Two) questions   | 2 × 5        |
| 1.<br>2.<br>3. | If G be a non-commutative group with centre Z, show that the quotient group of $G/Z$ is non-cyclic.<br>Show that the intersection of two normal subgroups of a group G is again a normal subgroup of G.<br>Show that in a ring $(\mathbb{Z}_n, +, \cdot)$ an element $\overline{m}$ is a unit if and only if $gcd(m, n) = 1$ . |              |
|                | END OF QUESTION FOR MATHEMATICS GENERAL [PROGRAMME] COURSE   |              |
|                | Question for students with Mathematics as SEC ; Full Marks = 05<br>G - SEC - T - 2A  | 05           |
|                | Answer any 1 (One) question  | $1 \times 5$ |
| 1.<br>2.       | <ul> <li>G is a simple graph with n vertices, where n ≥ 3 If deg(v) ≥ {n}/{2} for each vertex v, then the graph G is Hamiltonian graph.</li> <li>Draw the following:</li> <li>(a) A 3-regular graph of order at least 5;</li> <li>(b) A bipartite graph of order 6.</li> </ul>   | [2+3]        |